

Title: A PDE system modeling the growth of phytoplankton consuming inorganic carbon with internal storage in a water column

Speaker: Sze-Bi Hsu, National Tsing-Hua University, Taiwan

Abstract:

In this talk we shall discuss the effect of global warming on the growth of phytoplankton in the ocean and lakes. We present a system of reaction-diffusion equations which models the growth of a single species population consuming inorganic carbon that is stored internally in a poorly mixed habitat. Inorganic carbon takes the forms of "CO₂" (dissolved CO₂ and carbonic acid) and "CARB" (bicarbonate and carbonate ions), which are substitutable in their effects on algal growth. We apply a generalized Krein-Rutman Theorem involving two different cones by Mallet-Paret & R.D. Nussbaum in 2010 to establish a threshold type result on the extinction/persistence of the species in terms of the sign of a principal eigenvalue associated with a nonlinear eigenvalue problem.

This talk is based on my recent work jointly with Drs. Feng-Bin Wang (Chang-Gung University) and King-Yeung Lam (Ohio State University).